

# Specific Heat Capacity at Constant Volume for $\{x\text{NH}_3 + (1 - x)\text{H}_2\text{O}\}$ at Temperatures from 300 to 520 K and Pressures to 20 MPa

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Specific heat capacities at constant volume ( $c_V$ ) of  $\{x\text{NH}_3 + (1 - x)\text{H}_2\text{O}\}$  ( $x \approx 0.7, 0.8, 0.9$ ) mixtures were measured with an adiabatic calorimeter. Temperatures ranged from 300 K to 520 K, and pressures ranged from 3 MPa to 20 MPa. Measurements were conducted on single-phase liquid and compressed gaseous samples. The mixtures were gravimetrically prepared from high-purity substances and verified by chemical analysis. Density was reported for initial and final end points during each calorimetric experiment. The principal sources of uncertainty are the temperature rise measurement and the change-of-volume work adjustment. The expanded relative uncertainty (with a coverage factor  $k = 2$  and thus a 2-standard-deviation estimate) for  $c_V$  is estimated to be 1% for liquid phase and 4% for gaseous results, and for density it is 0.2%.

## Introduction

Thermodynamic properties of a fluid may be calculated from a knowledge of its ideal-gas properties and an accurate equation of state. Heat capacities derived in this manner, however, often lack sufficient accuracy since the calculation involves integration of the isochoric curvature  $(\partial^2 p / \partial T^2)_\rho$  as in the equation

$$c_V - c_V^\circ = -T \int_0^\rho \left( \frac{\partial^2 P}{\partial T^2} \right)_\rho \frac{d\rho}{\rho^2} \quad (1)$$

where  $c_V^\circ$  is the ideal-gas heat capacity. The quantity  $(\partial^2 p / \partial T^2)_\rho$  is known to possess small absolute values except in the vicinity of the critical point and is very difficult to measure accurately. For compressed liquid states, additional data are required to apply eq 1, including the vapor pressure and enthalpy of vaporization or heat capacity of the saturated liquid. Direct measurements of heat capacities provide useful checks on calculated heat capacities when they are available along a path traversing the temperature range of interest.

Tillner-Roth and Friend (1998a) have carried out a survey of the available literature for  $\text{NH}_3 + \text{H}_2\text{O}$  mixtures. Their survey cites a total of three other publications (Chan and Giauque, 1964; Hildenbrand and Giauque, 1953; Wrewsky and Kaigorodoff, 1924) of heat capacity data and one publication of saturated-liquid enthalpy by Zinner (1934). The temperature range covered by published heat capacity data is 183 K to 334 K, with  $\text{NH}_3$  compositions between 0.01 and 0.67 mole fraction. No heat capacities were found for  $\text{NH}_3$ -rich compositions at mole fractions above 0.67 or at temperatures above 334 K.

In this paper, heat capacities are reported for single-phase liquid and gaseous states from near ambient temperature to the upper limit of the apparatus (520 K). In addition, densities calculated from sample mass measure-

ments and the volume of the calorimeter bomb are reported.

## Experimental Section

**Materials.** High-purity samples of  $\text{NH}_3$  and  $\text{H}_2\text{O}$  were obtained to prepare the mixtures. The  $\text{NH}_3$  samples were drawn from a supply cylinder of anhydrous  $\text{NH}_3$ , with a certified minimum liquid purity of 0.9999 mole fraction. A gas chromatographic analysis confirmed this purity. Our  $\text{H}_2\text{O}$  supply was twice distilled in our laboratories and has a minimum purity of 0.9999 mole fraction.

The three mixtures of this study were prepared gravimetrically in clean, dry diaphragm cells constructed of Type-316 stainless steel. Each cell has a sample cavity above the diaphragm and a water-filled cavity below it, each having a volume of 100  $\text{cm}^3$ . Water could be metered with a dual-piston pump into the lower cavity to raise and lower the diaphragm that separates the two chambers.

Prior to preparation of a mixture, calculations were made of the masses of  $\text{NH}_3$  ( $M = 17.0303 \text{ g}\cdot\text{mol}^{-1}$ ) and  $\text{H}_2\text{O}$  ( $M = 18.0153 \text{ g}\cdot\text{mol}^{-1}$ ) required for the target composition. Then, each component was introduced to the upper chamber while the whole cell rested on an electronic platform balance capable of 0.1 g resolution. After each component was introduced, the whole cell was accurately weighed with a 25 kg capacity dual-pan balance whose resolution is 0.001 g and uncertainty is 0.005 g. After the final weighing, enough water was pumped into the lower chamber to pressurize the mixture above the diaphragm to 15 MPa. This pressure is well above the calculated bubble point pressure of the mixtures and thus promotes mixing of the two phases. Owing to the negative sign of the excess volume for  $\text{NH}_3 + \text{H}_2\text{O}$  mixtures, the pressure fell as the sample was mixing. By monitoring the falling pressure of the water in the lower chamber, it was possible to determine that mixing was almost complete within 1 h. To ensure complete homogenization, each  $\text{NH}_3 + \text{H}_2\text{O}$  mixture was then held for 2 weeks during which no further drift of pressure was detected. Following this holding period, each mixture was used in experiments. The masses and com-

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**Table 1. Component Mass  $m$ , Mass Fraction  $\text{NH}_3$   $w$ , and Mole Fraction  $x$  of  $\{x\text{NH}_3 + (1-x)\text{H}_2\text{O}\}$  Mixtures Used in This Study**

| designation | $m(\text{NH}_3)/\text{g}$ | $m(\text{H}_2\text{O})/\text{g}$ | $x$      | $w$      |
|-------------|---------------------------|----------------------------------|----------|----------|
| 80/20       | 56.623                    | 13.372                           | 0.817 50 | 0.808 96 |
| 90/10       | 57.676                    | 6.434                            | 0.904 60 | 0.899 64 |
| 70/30       | 58.913                    | 24.936                           | 0.714 22 | 0.702 61 |

positions of the mixtures used in this study are presented in Table 1.

**Measurements.** A twin-bomb adiabatic calorimeter was used for these measurements. Since this apparatus has been described in detail by Magee et al. (1998), only a brief discussion will be given here. A spherical bomb contains a sample of well-established mass. A second identical bomb serves as a reference. The volume of the bomb, approximately 70 cm<sup>3</sup>, is a function of temperature and pressure. A platinum resistance thermometer is attached to the bomb for the temperature measurement. Temperatures are reported on the ITS-90, after conversions from the original calibration on the IPTS-68. Pressures are measured with an oscillating quartz crystal pressure transducer with a 0–70 MPa range. Adiabatic conditions are ensured by a high vacuum ( $3 \times 10^{-3}$  Pa) in the vacuum space surrounding each calorimeter, by a temperature-controlled radiation shield, and by a temperature-controlled guard ring which thermally anchors the filling capillary and the lead wires to the bomb.

For the heat capacity measurement, a precisely determined electrical energy ( $Q$ ) is applied and the resulting temperature rise ( $\Delta T = T_2 - T_1$ ) is measured. We obtain the heat capacity from

$$c_V = \left( \frac{\partial U}{\partial T} \right)_V \cong \frac{\Delta Q - \Delta Q_0 - W_{pV}}{m\Delta T} \quad (2)$$

where  $U$  is the internal energy,  $\Delta Q_0 = Q_{0,\text{sam}} - Q_{0,\text{ref}}$  is the energy difference between the sample and reference sides when both bombs are empty,  $\Delta Q = Q_{\text{sam}} - Q_{\text{ref}}$  refers to the energy added during an experiment with a sample,  $W_{pV}$  is the change-of-volume work due to the slight dilation of the bomb, and  $m$  is the mass of substance enclosed in the sample bomb. In this work, the bomb was charged with sample up to the ( $p$ ,  $T$ ) conditions of the highest-density isochore to be measured. The bomb and its contents were cooled to a starting temperature in the single-phase liquid region. Then, measurements were performed in that region with increasing temperature until either the upper temperature (520 K) or pressure limit (20 MPa) was attained. At the completion of a run, a small part of the sample was cryopumped into a lightweight cylinder. The next run was started with a lower density. When the runs were completed, the remaining sample was discharged and weighed. A series of such runs from different fillings completes the investigation of the ( $p$ ,  $T$ ,  $c_V$ ) surface. Each mass increment was determined from the difference of weighings of the lightweight cylinder made with a sensitive ( $10^{-3}$  g) balance. Small adjustments were made to each mass increment for changes in air buoyancy. The sample mass for each run was determined from the sum of the appropriate mass increments.

**Assessment of Uncertainties.** Uncertainty in the  $c_V$  determination has been discussed in detail (Magee et al., 1998). Primarily, the accuracy of this method is limited by the uncertainty involved in the temperature rise measurement and the change-of-volume work adjustment. We use a definition for the expanded uncertainty that is two times the standard uncertainty (i.e., a coverage factor  $k =$

**Table 2. Expanded Uncertainties of the Temperature, Pressure, Mass, Volume, Composition, Density, Energy, Change-of-Volume Work, and Specific Heat Capacity**

|                        |                      |                        |                       |
|------------------------|----------------------|------------------------|-----------------------|
| temperature            |                      | density                | 0.2%                  |
| absolute               | 0.03 K               | energy                 |                       |
| difference, $\Delta T$ | $7 \times 10^{-4}$ K | power                  | 0.02%                 |
| pressure               | 0.007 MPa            | difference, $\Delta Q$ | 0.5 J·K <sup>-1</sup> |
| mass                   | 0.002 g              | change-of-volume work  | 2%                    |
| volume                 | 0.07 cm <sup>3</sup> | specific heat capacity |                       |
| composition,           | 0.0002               | liquid                 | 1%                    |
| mass fraction          |                      | vapor                  | 4%                    |

2 and thus a 2-standard-deviation estimate). The expanded uncertainties of the original measurements and the resulting combined uncertainties are shown in Table 2.

### Heat Capacity and Density Results

As mentioned in the discussion of eq 2, adjustments should be applied to the raw heat capacity data for the change-of-volume work of the bomb. During a measurement sequence, the volume of the bomb varies with temperature and pressure in accordance with formulas reported previously (Magee et al., 1998). The term  $W_{pV}$  is an important adjustment since the bomb is thin-walled. Referring to Goodwin and Weber (1969), we can obtain the work from

$$W_{pV} = \left( T_2 \left( \frac{\partial p}{\partial T} \right)_{V_2} - \frac{1}{2} \Delta p \right) \Delta V \quad (3)$$

where  $\Delta p = p_2 - p_1$  is the pressure rise and  $\Delta V = V_2 - V_1$  is the change of volume. The pressure derivative is obtained from an equation of state. Accurate values for the pressure derivative were required, since this quantity has a significant influence on the adjustment for the change of volume work. Estimates of this derivative were calculated with an equation for the Helmholtz energy of  $\text{NH}_3 + \text{H}_2\text{O}$  mixtures developed by Tillner-Roth and Friend (1998b).

A minor adjustment is applied to the mass enclosed in the bomb. The total mass of the sample is corrected by deducting the mass residing in the noxious volume, which consists of the combined volumes of the connecting tubing, the charging valve body, and the pressure transducer. In total, the noxious volume is approximately 0.4% of the bomb volume. This amount is calculated from densities calculated with an equation of state (Tillner-Roth and Friend, 1998b) and the noxious volume obtained from previous calibrations (Magee et al., 1998).

The heat capacity data  $c_V$  of each run are presented in Table 3 for a total of 303 single-phase liquid and gaseous states. The final temperature ( $T$ , ITS-90) and pressure  $p$  of the heating interval are presented. The densities  $\rho$  of 359 states were calculated from the measured sample mass and the calibrated bomb volume at the measured temperatures and pressures. The measurements in Table 3 are presented in the order ( $x \approx 0.8, 0.9, \text{ and } 0.7$ ) in which the experiments were carried out. For each filling, up to five replicate runs were carried out in the same ranges of temperature and pressure. Table 3 presents the mean  $c_V$  of the replicate experiments at each temperature, calculated after dropping any  $c_V$  values that fell outside of the 95% confidence interval. The experimental densities and heat capacities are presented in the tables alongside values calculated with the formulation developed by Tillner-Roth and Friend (1998b).

Figures 1, 3, and 5 show the ranges of the measured temperatures and pressures along isochores and their relationship to calculated dew-bubble curves, for each composition. The measured pressures range up to 20 MPa,

**Table 3. Experimental Densities  $\rho_{\text{exp}}$  and Heat Capacities  $c_V$  for  $\{x\text{NH}_3 + (1-x)\text{H}_2\text{O}\}$ :  $x$ , mass fraction;  $T$ , Temperature on ITS-90;  $p$ , pressure;  $\rho_{\text{calc}}$  and  $c_{V,\text{calc}}$  are Calculated with the Model of Tillner-Roth and Friend (1998b); dev. = 100 (exp - calc)/calc**

| $T/K$         | $p/\text{MPa}$ | $\rho_{\text{exp}}/\text{g}\cdot\text{cm}^3$ | $\rho_{\text{calc}}/\text{g}\cdot\text{cm}^3$ | dev.  | $c_V(\text{no.1})^a$ | $c_V(\text{no.2})$ | $c_V(\text{no.3})$ | $c_V(\text{no.4})$ | $c_V(\text{no.5})$ | $c_{V,\text{avg}}$ | $c_{V,\text{calc}}$ | dev.  |
|---------------|----------------|--|---|-------|----------------------|--------------------|--------------------|--------------------|--------------------|--------------------|---------------------|-------|
| $x = 0.80896$ |                |  |   |       |                      |                    |                    |                    |                    |                    |                     |       |
| 301           | 5.37           | 0.69131                                      | 0.69014                                       | 0.17  |                      |                    |                    |                    |                    |                    |                     |       |
| 302           | 7.10           | 0.69112                                      | 0.69013                                       | 0.14  | 3.348                | 3.337              |                    |                    |                    | 3.343              | 3.362               | -0.58 |
| 303           | 8.84           | 0.69092                                      | 0.69011                                       | 0.12  | 3.336                | 3.330              |                    |                    |                    | 3.333              | 3.354               | -0.63 |
| 304           | 10.57          | 0.69073                                      | 0.69008                                       | 0.09  | 3.323                | 3.339              |                    |                    |                    | 3.331              | 3.346               | -0.45 |
| 305           | 12.30          | 0.69053                                      | 0.69004                                       | 0.07  | 3.339                | 3.336              |                    |                    |                    | 3.338              | 3.338               | -0.01 |
| 306           | 14.03          | 0.69034                                      | 0.69000                                       | 0.05  | 3.340                | 3.333              |                    |                    |                    | 3.336              | 3.331               | 0.17  |
| 307           | 15.76          | 0.69014                                      | 0.68995                                       | 0.03  | 3.348                | 3.362              |                    |                    |                    | 3.355              | 3.323               | 0.96  |
| 308           | 17.48          | 0.68995                                      | 0.68990                                       | 0.01  | 3.357                | 3.353              |                    |                    |                    | 3.355              | 3.316               | 1.18  |
| 309           | 19.20          | 0.68975                                      | 0.68983                                       | -0.01 | 3.355                | 3.344              |                    |                    |                    | 3.350              | 3.309               | 1.22  |
| 320           | 3.01           | 0.66464                                      | 0.66317                                       | 0.22  |                      |                    |                    |                    |                    |                    |                     |       |
| 321           | 4.59           | 0.66447                                      | 0.66321                                       | 0.19  |                      | 3.175              | 3.202              |                    |                    | 3.189              | 3.354               | -4.91 |
| 322           | 6.16           | 0.66430                                      | 0.66324                                       | 0.16  |                      | 3.202              | 3.184              |                    |                    | 3.193              | 3.344               | -4.53 |
| 323           | 7.72           | 0.66412                                      | 0.66325                                       | 0.13  |                      | 3.205              | 3.200              |                    |                    | 3.202              | 3.335               | -3.98 |
| 324           | 9.28           | 0.66395                                      | 0.66326                                       | 0.10  |                      | 3.209              | 3.225              |                    |                    | 3.217              | 3.326               | -3.28 |
| 325           | 10.85          | 0.66378                                      | 0.66326                                       | 0.08  |                      | 3.235              | 3.242              |                    |                    | 3.239              | 3.318               | -2.38 |
| 326           | 12.41          | 0.66361                                      | 0.66325                                       | 0.05  | 3.248                | 3.249              | 3.265              |                    |                    | 3.254              | 3.309               | -1.67 |
| 327           | 13.96          | 0.66344                                      | 0.66324                                       | 0.03  | 3.277                | 3.272              | 3.280              |                    |                    | 3.276              | 3.301               | -0.76 |
| 328           | 15.52          | 0.66326                                      | 0.66321                                       | 0.01  | 3.274                | 3.273              | 3.259              |                    |                    | 3.268              | 3.293               | -0.76 |
| 329           | 17.07          | 0.66309                                      | 0.66318                                       | -0.01 | 3.247                | 3.283              | 3.294              |                    |                    | 3.275              | 3.286               | -0.33 |
| 330           | 18.62          | 0.66292                                      | 0.66315                                       | -0.03 | 3.294                | 3.286              | 3.299              |                    |                    | 3.293              | 3.278               | 0.46  |
| 343           | 5.76           | 0.63397                                      | 0.63270                                       | 0.20  |                      |                    |                    |                    |                    |                    |                     |       |
| 344           | 7.14           | 0.63382                                      | 0.63277                                       | 0.17  | 3.286                | 3.233              | 3.223              |                    |                    | 3.247              | 3.3223              | -2.26 |
| 345           | 8.51           | 0.63367                                      | 0.63281                                       | 0.14  | 3.256                | 3.268              | 3.247              |                    |                    | 3.257              | 3.3125              | -1.68 |
| 346           | 9.89           | 0.63353                                      | 0.63285                                       | 0.11  | 3.236                |                    |                    |                    |                    | 3.236              | 3.3031              | -2.03 |
| 347           | 11.26          | 0.63338                                      | 0.63288                                       | 0.08  | 3.274                |                    |                    |                    |                    | 3.274              | 3.2939              | -0.6  |
| 348           | 12.63          | 0.63323                                      | 0.63290                                       | 0.05  |                      | 3.257              | 3.250              |                    |                    | 3.253              | 3.2849              | -0.97 |
| 349           | 14.00          | 0.63308                                      | 0.63291                                       | 0.03  | 3.269                |                    | 3.249              |                    |                    | 3.259              | 3.2762              | -0.53 |
| 350           | 15.37          | 0.63293                                      | 0.63292                                       | 0.00  | 3.248                |                    | 3.257              |                    |                    | 3.253              | 3.2677              | -0.46 |
| 351           | 16.74          | 0.63279                                      | 0.63292                                       | -0.02 | 3.272                | 3.231              | 3.246              |                    |                    | 3.250              | 3.2595              | -0.3  |
| 352           | 18.11          | 0.63264                                      | 0.63291                                       | -0.04 | 3.242                | 3.225              | 3.228              |                    |                    | 3.231              | 3.2515              | -0.62 |
| 353           | 19.48          | 0.63249                                      | 0.63289                                       | -0.06 | 3.273                | 3.234              | 3.265              |                    |                    | 3.257              | 3.2436              | 0.42  |
| 361           | 6.78           | 0.60678                                      | 0.60536                                       | 0.24  |                      |                    |                    |                    |                    | 3.257              | 3.2436              | 0.42  |
| 362           | 8.00           | 0.60665                                      | 0.60545                                       | 0.20  | 3.205                | 3.203              |                    |                    |                    | 3.204              | 3.314               | -3.30 |
| 363           | 9.22           | 0.60652                                      | 0.60553                                       | 0.16  | 3.198                | 3.177              |                    |                    |                    | 3.188              | 3.303               | -3.50 |
| 364           | 10.44          | 0.60639                                      | 0.60560                                       | 0.13  | 3.179                | 3.194              |                    |                    |                    | 3.186              | 3.293               | -3.25 |
| 365           | 11.65          | 0.60626                                      | 0.60566                                       | 0.10  | 3.197                | 3.205              |                    |                    |                    | 3.201              | 3.283               | -2.51 |
| 366           | 12.87          | 0.60613                                      | 0.60570                                       | 0.07  | 3.206                | 3.203              |                    |                    |                    | 3.204              | 3.274               | -2.12 |
| 367           | 14.09          | 0.60600                                      | 0.60574                                       | 0.04  | 3.193                | 3.213              |                    |                    |                    | 3.203              | 3.264               | -1.89 |
| 368           | 15.30          | 0.60588                                      | 0.60577                                       | 0.02  | 3.191                | 3.203              |                    |                    |                    | 3.197              | 3.255               | -1.79 |
| 369           | 16.52          | 0.60575                                      | 0.60579                                       | -0.01 | 3.220                | 3.239              |                    |                    |                    | 3.230              | 3.247               | -0.52 |
| 370           | 17.73          | 0.60562                                      | 0.60580                                       | -0.03 |                      | 3.245              |                    |                    |                    | 3.245              | 3.238               | 0.23  |
| 371           | 18.97          | 0.60549                                      | 0.60584                                       | -0.06 | 3.254                |                    |                    |                    |                    | 3.254              | 3.230               | 0.75  |
| 402           | 10.47          | 0.53653                                      | 0.53337                                       | 0.59  |                      |                    |                    |                    |                    |                    |                     |       |
| 403           | 11.34          | 0.53644                                      | 0.53351                                       | 0.55  |                      | 3.179              |                    |                    |                    | 3.179              | 3.329               | -4.51 |
| 404           | 12.21          | 0.53635                                      | 0.53364                                       | 0.51  |                      | 3.139              |                    |                    |                    | 3.139              | 3.317               | -5.36 |
| 405           | 13.07          | 0.53626                                      | 0.53375                                       | 0.47  |                      | 3.182              |                    |                    |                    | 3.182              | 3.305               | -3.71 |
| 406           | 13.94          | 0.53617                                      | 0.53385                                       | 0.44  | 3.153                | 3.154              | 3.162              |                    |                    | 3.156              | 3.293               | -4.16 |
| 407           | 14.81          | 0.53609                                      | 0.53394                                       | 0.40  | 3.154                | 3.149              | 3.166              |                    |                    | 3.156              | 3.282               | -3.83 |
| 408           | 15.68          | 0.53600                                      | 0.53401                                       | 0.37  | 3.197                | 3.202              | 3.190              |                    |                    | 3.196              | 3.271               | -2.29 |
| 409           | 16.55          | 0.53591                                      | 0.53408                                       | 0.34  | 3.168                | 3.195              | 3.183              |                    |                    | 3.182              | 3.261               | -2.42 |
| 410           | 17.42          | 0.53582                                      | 0.53413                                       | 0.32  | 3.205                | 3.185              | 3.162              |                    |                    | 3.184              | 3.250               | -2.05 |
| 411           | 18.30          | 0.53573                                      | 0.53419                                       | 0.29  | 3.185                | 3.181              | 3.152              |                    |                    | 3.173              | 3.240               | -2.09 |
| 412           | 19.17          | 0.53564                                      | 0.53423                                       | 0.26  | 3.156                | 3.199              | 3.195              |                    |                    | 3.183              | 3.231               | -1.46 |
| 442           | 15.33          | 0.44355                                      | 0.43878                                       | 1.09  |                      |                    |                    |                    |                    |                    |                     |       |
| 443           | 15.86          | 0.44349                                      | 0.43866                                       | 1.10  | 3.455                |                    |                    |                    |                    | 3.455              | 3.405               | 1.47  |
| 444           | 16.40          | 0.44344                                      | 0.43860                                       | 1.10  | 3.413                | 3.440              | 3.422              |                    |                    | 3.425              | 3.391               | 0.99  |
| 445           | 16.93          | 0.44339                                      | 0.43847                                       | 1.12  | 3.492                | 3.455              | 3.443              |                    |                    | 3.463              | 3.378               | 2.52  |
| 446           | 17.47          | 0.44334                                      | 0.43833                                       | 1.14  | 3.459                | 3.400              | 3.420              |                    |                    | 3.426              | 3.365               | 1.82  |
| 447           | 18.00          | 0.44329                                      | 0.43821                                       | 1.16  | 3.457                | 3.432              | 3.432              |                    |                    | 3.440              | 3.352               | 2.63  |
| 448           | 18.54          | 0.44323                                      | 0.43808                                       | 1.17  | 3.398                | 3.385              | 3.432              |                    |                    | 3.405              | 3.340               | 1.96  |
| 449           | 19.08          | 0.44318                                      | 0.43796                                       | 1.19  | 3.494                | 3.402              | 3.470              |                    |                    | 3.455              | 3.328               | 3.84  |
| 450           | 19.63          | 0.44313                                      | 0.43784                                       | 1.21  | 3.405                |                    | 3.436              |                    |                    | 3.420              | 3.316               | 3.15  |
| 492           | 13.60          | 0.09657                                      | 0.09624                                       | 0.34  |                      |                    |                    |                    |                    |                    |                     |       |
| 493           | 13.68          | 0.09656                                      | 0.09629                                       | 0.28  |                      |                    |                    |                    |                    |                    |                     |       |
| 494           | 13.75          | 0.09656                                      | 0.09632                                       | 0.25  |                      |                    |                    |                    |                    |                    |                     |       |
| 495           | 13.83          | 0.09655                                      | 0.09634                                       | 0.22  |                      |                    |                    |                    |                    |                    |                     |       |
| 496           | 13.91          | 0.09655                                      | 0.09638                                       | 0.18  |                      |                    |                    |                    |                    |                    |                     |       |
| 497           | 13.99          | 0.09654                                      | 0.09642                                       | 0.13  | 3.288                |                    | 3.603              |                    |                    | 3.445              | 2.797               | 23.17 |
| 498           | 14.07          | 0.09654                                      | 0.09642                                       | 0.13  |                      |                    | 3.402              |                    |                    | 3.402              | 2.790               | 21.94 |
| 499           | 14.15          | 0.09653                                      | 0.09646                                       | 0.07  |                      |                    | 3.396              |                    |                    | 3.396              | 2.783               | 22.04 |
| 500           | 14.22          | 0.09653                                      | 0.09649                                       | 0.04  |                      |                    |                    |                    | 3.382              | 3.382              | 2.776               | 21.81 |
| 501           | 14.30          | 0.09652                                      | 0.09652                                       | 0.00  |                      | 3.422              | 3.456              | 3.396              | 3.347              | 3.405              | 2.769               | 22.96 |
| 502           | 14.38          | 0.09652                                      | 0.09655                                       | -0.03 |                      |                    |                    | 3.568              | 3.450              | 3.509              | 2.763               | 27.00 |

Table 3 (Continued)

| <i>T/K</i>      | <i>p/MPa</i> | $\rho_{\text{exp}}/\text{g}\cdot\text{cm}^3$ | $\rho_{\text{calc}}/\text{g}\cdot\text{cm}^3$ | dev.  | $c_V(\text{no.1})^a$ | $c_V(\text{no.2})$ | $c_V(\text{no.3})$ | $c_V(\text{no.4})$ | $c_V(\text{no.5})$ | $c_{V,\text{avg}}$ | $c_{V,\text{calc}}$ | dev.  |
|-----------------|--------------|--|---|-------|----------------------|--------------------|--------------------|--------------------|--------------------|--------------------|---------------------|-------|
| 503             | 14.46        | 0.096 51                                     | 0.096 57                                      | -0.06 |                      | 3.420              | 3.536              |                    | 3.333              | 3.430              | 2.756               | 24.46 |
| 504             | 14.53        | 0.096 51                                     | 0.096 60                                      | -0.10 |                      |                    | 3.368              | 3.383              |                    | 3.376              | 2.750               | 22.75 |
| 505             | 14.61        | 0.096 50                                     | 0.096 63                                      | -0.14 | 3.356                |                    | 3.456              | 3.414              |                    | 3.409              | 2.744               | 24.22 |
| 506             | 14.69        | 0.096 50                                     | 0.096 66                                      | -0.16 | 3.306                | 3.445              |                    | 3.388              | 3.321              | 3.365              | 2.738               | 22.89 |
| 507             | 14.77        | 0.096 49                                     | 0.096 68                                      | -0.19 | 3.437                | 3.435              | 3.290              |                    | 3.488              | 3.412              | 2.732               | 24.90 |
| 508             | 14.84        | 0.096 48                                     | 0.096 70                                      | -0.22 | 3.353                |                    |                    | 3.431              | 3.417              | 3.400              | 2.726               | 24.73 |
| 509             | 14.92        | 0.096 48                                     | 0.096 73                                      | -0.26 | 3.209                | 3.303              | 3.183              |                    |                    | 3.232              | 2.721               | 18.77 |
| 510             | 15.00        | 0.096 47                                     | 0.096 74                                      | -0.28 |                      | 3.291              |                    | 3.282              |                    | 3.286              | 2.715               | 21.03 |
| 511             | 15.07        | 0.096 47                                     | 0.096 77                                      | -0.31 |                      | 3.291              | 3.370              | 3.446              | 3.439              | 3.387              | 2.710               | 24.99 |
| 512             | 15.15        | 0.096 46                                     | 0.096 79                                      | -0.35 |                      |                    | 3.312              | 3.370              | 3.292              | 3.324              | 2.704               | 22.93 |
| 513             | 15.23        | 0.096 46                                     | 0.096 82                                      | -0.37 |                      | 3.211              |                    | 3.376              | 3.433              | 3.340              | 2.699               | 23.74 |
| 514             | 15.30        | 0.096 45                                     | 0.096 83                                      | -0.39 |                      |                    | 3.161              |                    |                    | 3.161              | 2.694               | 17.35 |
| 515             | 15.38        | 0.096 45                                     | 0.096 86                                      | -0.42 |                      | 3.361              |                    | 3.125              | 3.408              | 3.298              | 2.689               | 22.64 |
| 516             | 15.45        | 0.096 44                                     | 0.096 87                                      | -0.45 | 3.267                | 3.243              | 3.095              | 3.125              | 3.092              | 3.164              | 2.684               | 17.89 |
| 517             | 15.53        | 0.096 44                                     | 0.096 89                                      | -0.46 |                      | 3.073              | 3.319              | 3.325              |                    | 3.239              | 2.679               | 20.89 |
| 518             | 15.60        | 0.096 43                                     | 0.096 91                                      | -0.49 |                      |                    |                    | 3.321              | 2.949              | 3.135              | 2.675               | 17.20 |
| 519             | 15.68        | 0.096 43                                     | 0.096 93                                      | -0.51 |                      | 3.047              |                    |                    |                    | 3.047              | 2.670               | 14.12 |
| 520             | 15.76        | 0.096 42                                     | 0.096 95                                      | -0.55 |                      | 3.339              | 3.025              | 3.291              |                    | 3.218              | 2.666               | 20.72 |
| 521             | 15.83        | 0.096 42                                     | 0.096 96                                      | -0.56 | 3.006                |                    |                    |                    | 3.247              | 3.127              | 2.661               | 17.49 |
| 522             | 15.91        | 0.096 41                                     | 0.096 98                                      | -0.59 |                      | 3.125              |                    | 3.107              |                    | 3.116              | 2.657               | 17.26 |
| $x = 0.899\ 64$ |              |  |   |       |                      |                    |                    |                    |                    |                    |                     |       |
| 301             | 3.63         | 0.648 43                                     | 0.646 39                                      | 0.32  |                      |                    |                    |                    |                    |                    |                     |       |
| 302             | 5.24         | 0.648 26                                     | 0.646 39                                      | 0.29  |                      |                    |                    |                    |                    |                    |                     |       |
| 303             | 6.84         | 0.648 09                                     | 0.646 38                                      | 0.26  |                      | 3.077              |                    |                    | 3.077              | 3.167              | -2.83               |       |
| 304             | 8.44         | 0.647 92                                     | 0.646 36                                      | 0.24  | 3.090                | 3.061              |                    |                    | 3.075              | 3.160              | -2.67               |       |
| 305             | 10.04        | 0.647 75                                     | 0.646 34                                      | 0.22  | 3.086                | 3.104              |                    |                    | 3.095              | 3.153              | -1.86               |       |
| 306             | 11.63        | 0.647 57                                     | 0.646 31                                      | 0.19  | 3.123                | 3.061              |                    |                    | 3.092              | 3.147              | -1.76               |       |
| 307             | 13.23        | 0.647 4                                      | 0.646 29                                      | 0.17  | 3.094                | 3.086              |                    |                    | 3.090              | 3.141              | -1.63               |       |
| 308             | 14.81        | 0.647 23                                     | 0.646 24                                      | 0.15  | 3.063                | 3.073              |                    |                    | 3.068              | 3.135              | -2.14               |       |
| 309             | 16.40        | 0.647 06                                     | 0.646 20                                      | 0.13  | 3.085                | 3.069              |                    |                    | 3.077              | 3.129              | -1.68               |       |
| 310             | 17.99        | 0.646 89                                     | 0.646 16                                      | 0.11  | 3.058                | 3.062              |                    |                    | 3.060              | 3.124              | -2.05               |       |
| 311             | 19.58        | 0.646 72                                     | 0.646 11                                      | 0.09  | 3.092                | 3.090              |                    |                    | 3.091              | 3.118              | -0.87               |       |
| 321             | 5.74         | 0.621 61                                     | 0.619 82                                      | 0.29  |                      |                    |                    |                    |                    |                    |                     |       |
| 322             | 7.17         | 0.621 46                                     | 0.619 84                                      | 0.26  |                      |                    |                    |                    |                    |                    |                     |       |
| 323             | 8.60         | 0.621 31                                     | 0.619 85                                      | 0.24  | 3.0687               |                    |                    |                    | 3.069              | 3.134              | -2.10               |       |
| 324             | 10.02        | 0.621 16                                     | 0.619 85                                      | 0.21  | 3.0677               | 3.0707             |                    |                    | 3.069              | 3.128              | -1.86               |       |
| 325             | 11.44        | 0.621 01                                     | 0.619 85                                      | 0.19  | 3.0635               | 3.0729             |                    |                    | 3.068              | 3.121              | -1.68               |       |
| 326             | 12.86        | 0.620 86                                     | 0.619 84                                      | 0.16  | 3.0745               | 3.0742             |                    |                    | 3.074              | 3.114              | -1.28               |       |
| 327             | 14.28        | 0.620 71                                     | 0.619 83                                      | 0.14  | 3.0909               |                    |                    |                    | 3.091              | 3.108              | -0.54               |       |
| 328             | 15.70        | 0.620 56                                     | 0.619 80                                      | 0.12  | 3.0602               | 3.0656             |                    |                    | 3.063              | 3.102              | -1.25               |       |
| 329             | 17.12        | 0.620 41                                     | 0.619 78                                      | 0.10  | 3.0883               | 3.0821             |                    |                    | 3.085              | 3.096              | -0.34               |       |
| 330             | 18.53        | 0.620 27                                     | 0.619 75                                      | 0.08  | 3.0779               | 3.0850             |                    |                    | 3.081              | 3.090              | -0.27               |       |
| 340             | 4.52         | 0.590 39                                     | 0.588 45                                      | 0.33  |                      |                    |                    |                    |                    |                    |                     |       |
| 341             | 5.76         | 0.590 26                                     | 0.588 51                                      | 0.30  |                      |                    |                    |                    | 3.029              | 3.029              | 3.135               | -3.38 |
| 342             | 6.99         | 0.590 14                                     | 0.588 56                                      | 0.27  |                      | 2.984              |                    |                    | 2.984              | 3.127              | -4.58               |       |
| 343             | 8.22         | 0.590 01                                     | 0.588 59                                      | 0.24  |                      | 3.007              |                    |                    | 3.007              | 3.119              | -3.59               |       |
| 344             | 9.46         | 0.589 88                                     | 0.588 63                                      | 0.21  | 3.020                | 3.043              |                    |                    | 3.031              | 3.111              | -2.58               |       |
| 345             | 10.69        | 0.589 76                                     | 0.588 65                                      | 0.19  | 3.014                | 3.003              |                    |                    | 3.008              | 3.104              | -3.08               |       |
| 346             | 11.92        | 0.589 63                                     | 0.588 67                                      | 0.16  | 3.044                | 3.038              |                    |                    | 3.041              | 3.097              | -1.80               |       |
| 347             | 13.15        | 0.589 50                                     | 0.588 68                                      | 0.14  | 3.024                | 3.017              |                    |                    | 3.021              | 3.090              | -2.24               |       |
| 348             | 14.38        | 0.589 38                                     | 0.588 69                                      | 0.12  | 3.038                | 3.036              |                    |                    | 3.037              | 3.083              | -1.50               |       |
| 349             | 15.61        | 0.589 25                                     | 0.588 69                                      | 0.10  |                      | 3.045              |                    |                    | 3.045              | 3.076              | -1.03               |       |
| 350             | 16.83        | 0.589 12                                     | 0.588 68                                      | 0.07  | 3.036                | 3.036              |                    |                    | 3.070              | -1.10              |                     |       |
| 351             | 18.06        | 0.589 00                                     | 0.588 68                                      | 0.06  | 3.055                | 3.055              |                    |                    | 3.064              | -0.29              |                     |       |
| 352             | 19.29        | 0.588 87                                     | 0.588 66                                      | 0.04  | 3.023                | 3.023              |                    |                    | 3.058              | -1.13              |                     |       |
| 363             | 7.05         | 0.552 74                                     | 0.551 23                                      | 0.27  |                      |                    |                    |                    |                    |                    |                     |       |
| 364             | 8.08         | 0.552 64                                     | 0.551 30                                      | 0.24  |                      |                    |                    |                    |                    |                    |                     |       |
| 365             | 9.10         | 0.552 54                                     | 0.551 36                                      | 0.21  | 2.957                | 2.971              |                    |                    | 2.964              | 3.112              | -4.76               |       |
| 366             | 10.13        | 0.552 43                                     | 0.551 41                                      | 0.18  | 2.971                | 2.980              |                    |                    | 2.976              | 3.104              | -4.12               |       |
| 367             | 11.16        | 0.552 33                                     | 0.551 47                                      | 0.16  | 3.010                | 3.010              |                    |                    | 3.010              | 3.095              | -2.74               |       |
| 368             | 12.19        | 0.552 23                                     | 0.551 50                                      | 0.13  | 2.967                | 3.009              |                    |                    | 2.988              | 3.087              | -3.22               |       |
| 369             | 13.21        | 0.552 12                                     | 0.551 53                                      | 0.11  | 3.025                | 3.026              |                    |                    | 3.025              | 3.079              | -1.75               |       |
| 370             | 14.24        | 0.552 02                                     | 0.551 56                                      | 0.08  | 2.966                | 2.977              |                    |                    | 2.971              | 3.072              | -3.28               |       |
| 371             | 15.27        | 0.551 92                                     | 0.551 57                                      | 0.06  | 3.032                |                    |                    |                    | 3.032              | 3.065              | -1.08               |       |
| 372             | 16.29        | 0.551 82                                     | 0.551 59                                      | 0.04  | 2.993                | 3.008              |                    |                    | 3.000              | 3.058              | -1.87               |       |
| 373             | 17.32        | 0.551 71                                     | 0.551 59                                      | 0.02  | 3.038                | 3.026              |                    |                    | 3.032              | 3.051              | -0.61               |       |
| 374             | 18.35        | 0.551 61                                     | 0.551 60                                      | 0.00  | 2.990                | 3.000              |                    |                    | 2.995              | 3.044              | -1.62               |       |
| 375             | 19.37        | 0.551 51                                     | 0.551 59                                      | -0.01 | 3.007                | 3.016              |                    |                    | 3.012              | 3.037              | -0.85               |       |
| 401             | 11.35        | 0.474 99                                     | 0.474 88                                      | 0.02  |                      |                    |                    |                    |                    |                    |                     |       |
| 402             | 12.04        | 0.474 92                                     | 0.474 90                                      | 0.00  |                      |                    |                    |                    |                    |                    |                     |       |
| 403             | 12.72        | 0.474 85                                     | 0.474 91                                      | -0.01 |                      |                    |                    |                    |                    |                    |                     |       |
| 404             | 13.41        | 0.474 79                                     | 0.474 91                                      | -0.03 |                      |                    |                    |                    |                    |                    |                     |       |
| 405             | 14.09        | 0.474 72                                     | 0.474 91                                      | -0.04 |                      | 3.226              |                    |                    | 3.226              | 3.118              | 3.48                |       |
| 406             | 14.78        | 0.474 66                                     | 0.474 90                                      | -0.05 | 3.180                | 3.202              |                    |                    | 3.191              | 3.108              | 2.66                |       |
| 407             | 15.46        | 0.474 59                                     | 0.474 88                                      | -0.06 |                      | 3.173              | 3.211              |                    | 3.192              | 3.099              | 3.01                |       |
| 408             | 16.15        | 0.474 52                                     | 0.474 87                                      | -0.07 |                      | 3.165              | 3.177              |                    | 3.171              | 3.090              | 2.63                |       |

Table 3 (Continued)

| $T/K$ | $p/\text{MPa}$ | $\rho_{\text{exp}}/\text{g}\cdot\text{cm}^3$ | $\rho_{\text{calc}}/\text{g}\cdot\text{cm}^3$ | dev.  | $c_V(\text{no.1})^a$ | $c_V(\text{no.2})$ | $c_V(\text{no.3})$ | $c_V(\text{no.4})$ | $c_V(\text{no.5})$ | $c_{V,\text{avg}}$ | $c_{V,\text{calc}}$ | dev.  |
|-------|----------------|--|---|-------|----------------------|--------------------|--------------------|--------------------|--------------------|--------------------|---------------------|-------|
| 409   | 16.84          | 0.474 46                                     | 0.474 83                                      | -0.08 |                      | 3.152              | 3.158              |                    |                    | 3.155              | 3.081               | 2.40  |
| 410   | 17.53          | 0.474 39                                     | 0.474 81                                      | -0.09 | 3.163                | 3.166              | 3.148              |                    |                    | 3.159              | 3.073               | 2.81  |
| 411   | 18.23          | 0.474 32                                     | 0.474 77                                      | -0.10 |                      | 3.166              |                    |                    |                    | 3.166              | 3.064               | 3.32  |
| 412   | 18.92          | 0.474 26                                     | 0.474 74                                      | -0.10 | 3.150                | 3.185              | 3.156              |                    |                    | 3.163              | 3.056               | 3.51  |
| 413   | 19.62          | 0.474 19                                     | 0.474 70                                      | -0.11 | 3.135                | 3.133              |                    |                    |                    | 3.134              | 3.048               | 2.81  |
| 421   | 13.67          | 0.416 88                                     | 0.418 69                                      | -0.43 |                      |                    |                    |                    |                    |                    |                     |       |
| 422   | 14.16          | 0.416 84                                     | 0.418 48                                      | -0.39 |                      |                    |                    |                    |                    |                    |                     |       |
| 423   | 14.65          | 0.416 79                                     | 0.418 25                                      | -0.35 |                      | 3.354              |                    |                    |                    | 3.354              | 3.205               | 4.65  |
| 424   | 15.15          | 0.416 74                                     | 0.418 04                                      | -0.31 | 3.375                | 3.375              |                    |                    |                    | 3.375              | 3.194               | 5.68  |
| 425   | 15.65          | 0.416 70                                     | 0.417 84                                      | -0.27 | 3.310                | 3.400              |                    |                    |                    | 3.355              | 3.182               | 5.43  |
| 426   | 16.15          | 0.416 65                                     | 0.417 66                                      | -0.24 | 3.364                |                    |                    |                    |                    | 3.364              | 3.171               | 6.09  |
| 427   | 16.65          | 0.416 60                                     | 0.417 46                                      | -0.20 | 3.335                | 3.351              |                    |                    |                    | 3.343              | 3.160               | 5.77  |
| 428   | 17.16          | 0.416 56                                     | 0.417 28                                      | -0.17 |                      | 3.304              |                    |                    |                    | 3.304              | 3.150               | 4.89  |
| 429   | 17.66          | 0.416 51                                     | 0.417 10                                      | -0.14 | 3.276                | 3.358              |                    |                    |                    | 3.317              | 3.139               | 5.67  |
| 430   | 18.17          | 0.416 46                                     | 0.416 93                                      | -0.11 | 3.278                | 3.311              |                    |                    |                    | 3.294              | 3.129               | 5.28  |
| 431   | 18.68          | 0.416 42                                     | 0.416 76                                      | -0.08 | 3.320                | 3.289              |                    |                    |                    | 3.305              | 3.119               | 5.94  |
| 432   | 19.19          | 0.416 37                                     | 0.416 59                                      | -0.05 | 3.316                | 3.269              |                    |                    |                    | 3.293              | 3.110               | 5.88  |
| 433   | 19.70          | 0.416 32                                     | 0.416 42                                      | -0.02 | 3.256                | 3.247              |                    |                    |                    | 3.252              | 3.100               | 4.88  |
| 441   | 15.53          | 0.311 41                                     | 0.320 06                                      | -2.70 |                      |                    |                    |                    |                    |                    |                     |       |
| 442   | 15.81          | 0.311 38                                     | 0.318 69                                      | -2.29 | 4.203                |                    |                    |                    |                    | 4.203              | 3.426               | 22.68 |
| 443   | 16.09          | 0.311 36                                     | 0.317 41                                      | -1.91 | 4.286                |                    |                    |                    |                    | 4.286              | 3.412               | 25.65 |
| 444   | 16.37          | 0.311 34                                     | 0.316 25                                      | -1.55 | 4.129                |                    |                    |                    |                    | 4.129              | 3.397               | 21.54 |
| 445   | 16.66          | 0.311 32                                     | 0.315 23                                      | -1.24 | 4.111                |                    |                    |                    |                    | 4.111              | 3.382               | 21.55 |
| 446   | 16.94          | 0.311 3                                      | 0.314 28                                      | -0.95 | 4.027                |                    |                    |                    |                    | 4.027              | 3.368               | 19.58 |
| 447   | 17.23          | 0.311 28                                     | 0.313 40                                      | -0.68 | 3.991                |                    |                    |                    |                    | 3.991              | 3.353               | 19.02 |
| 448   | 17.52          | 0.311 25                                     | 0.312 57                                      | -0.42 | 3.926                |                    |                    |                    |                    | 3.926              | 3.338               | 17.59 |
| 449   | 17.81          | 0.311 23                                     | 0.311 85                                      | -0.20 | 3.990                |                    |                    |                    |                    | 3.990              | 3.324               | 20.03 |
| 450   | 18.10          | 0.311 21                                     | 0.311 15                                      | 0.02  | 3.879                |                    |                    |                    |                    | 3.879              | 3.310               | 17.20 |
| 451   | 18.39          | 0.311 18                                     | 0.310 49                                      | 0.22  | 3.818                |                    |                    |                    |                    | 3.818              | 3.295               | 15.86 |
| 452   | 18.69          | 0.311 16                                     | 0.309 91                                      | 0.40  | 3.727                |                    |                    |                    |                    | 3.727              | 3.281               | 13.59 |
| 453   | 18.98          | 0.311 14                                     | 0.309 36                                      | 0.58  | 3.744                |                    |                    |                    |                    | 3.744              | 3.268               | 14.59 |
| 454   | 19.28          | 0.311 11                                     | 0.308 85                                      | 0.73  | 3.616                |                    |                    |                    |                    | 3.616              | 3.254               | 11.12 |
| 455   | 19.57          | 0.311 09                                     | 0.308 35                                      | 0.89  | 3.639                |                    |                    |                    |                    | 3.639              | 3.241               | 12.29 |
| 456   | 19.87          | 0.311 07                                     | 0.307 91                                      | 1.03  | 3.566                |                    |                    |                    |                    | 3.566              | 3.228               | 10.49 |
| 448   | 15.65          | 0.241 27                                     | 0.258 58                                      | -6.69 |                      |                    |                    |                    |                    |                    |                     |       |
| 449   | 15.85          | 0.241 26                                     | 0.256 91                                      | -6.09 |                      |                    |                    |                    |                    |                    |                     |       |
| 450   | 16.06          | 0.241 25                                     | 0.255 46                                      | -5.56 |                      |                    |                    |                    |                    |                    |                     |       |
| 451   | 16.26          | 0.241 24                                     | 0.254 13                                      | -5.07 |                      |                    |                    |                    |                    |                    |                     |       |
| 452   | 16.47          | 0.241 23                                     | 0.252 95                                      | -4.63 | 4.307                | 4.494              | 4.488              |                    |                    | 4.430              | 3.448               | 28.46 |
| 453   | 16.68          | 0.241 22                                     | 0.251 87                                      | -4.23 | 4.266                | 4.476              | 4.397              |                    |                    | 4.380              | 3.429               | 27.72 |
| 454   | 16.89          | 0.241 21                                     | 0.250 88                                      | -3.85 | 4.245                | 4.437              | 4.364              |                    |                    | 4.349              | 3.411               | 27.50 |
| 455   | 17.10          | 0.241 19                                     | 0.249 91                                      | -3.49 | 4.173                | 4.230              | 4.253              |                    |                    | 4.219              | 3.392               | 24.37 |
| 456   | 17.31          | 0.241 18                                     | 0.249 03                                      | -3.15 | 4.148                | 3.997              | 4.082              |                    |                    | 4.076              | 3.374               | 20.80 |
| 457   | 17.52          | 0.241 17                                     | 0.248 23                                      | -2.84 | 3.935                | 4.184              | 4.051              |                    |                    | 4.057              | 3.356               | 20.88 |
| 458   | 17.73          | 0.241 16                                     | 0.247 47                                      | -2.55 | 3.924                | 3.967              | 4.047              |                    |                    | 3.979              | 3.338               | 19.19 |
| 459   | 17.94          | 0.241 14                                     | 0.246 80                                      | -2.29 | 3.978                | 3.905              | 3.942              |                    |                    | 3.942              | 3.321               | 18.68 |
| 460   | 18.15          | 0.241 13                                     | 0.246 16                                      | -2.04 |                      | 3.850              |                    |                    |                    | 3.850              | 3.305               | 16.49 |
| 461   | 18.36          | 0.241 11                                     | 0.245 57                                      | -1.82 | 3.866                | 3.809              | 4.065              |                    |                    | 3.913              | 3.288               | 18.99 |
| 462   | 18.58          | 0.241 10                                     | 0.244 99                                      | -1.59 | 3.784                | 3.820              | 3.857              |                    |                    | 3.820              | 3.273               | 16.73 |
| 463   | 18.79          | 0.241 08                                     | 0.244 48                                      | -1.39 | 3.725                | 3.777              | 3.942              |                    |                    | 3.815              | 3.258               | 17.11 |
| 464   | 19.00          | 0.241 07                                     | 0.243 98                                      | -1.19 | 3.652                | 3.689              | 3.723              |                    |                    | 3.688              | 3.243               | 13.73 |
| 465   | 19.22          | 0.241 06                                     | 0.243 52                                      | -1.01 | 3.701                | 3.772              | 3.752              |                    |                    | 3.741              | 3.228               | 15.90 |
| 466   | 19.43          | 0.241 04                                     | 0.243 09                                      | -0.84 | 3.663                | 3.609              | 3.667              |                    |                    | 3.646              | 3.214               | 13.44 |
| 467   | 19.64          | 0.241 02                                     | 0.242 69                                      | -0.69 | 3.541                | 3.669              | 3.628              |                    |                    | 3.613              | 3.201               | 12.88 |
| 468   | 19.86          | 0.241 01                                     | 0.242 29                                      | -0.53 | 3.470                | 3.545              | 3.615              |                    |                    | 3.544              | 3.188               | 11.17 |
| 452   | 15.30          | 0.191 87                                     | 0.209 13                                      | -8.25 |                      |                    |                    |                    |                    |                    |                     |       |
| 453   | 15.46          | 0.191 86                                     | 0.207 91                                      | -7.72 |                      |                    |                    |                    |                    |                    |                     |       |
| 454   | 15.63          | 0.191 85                                     | 0.206 86                                      | -7.26 |                      |                    |                    |                    |                    |                    |                     |       |
| 455   | 15.79          | 0.191 85                                     | 0.205 83                                      | -6.79 | 4.588                | 4.362              | 4.619              |                    |                    | 4.523              | 3.415               | 32.45 |
| 456   | 15.95          | 0.191 84                                     | 0.204 89                                      | -6.37 | 4.575                | 4.499              | 4.477              |                    |                    | 4.517              | 3.393               | 33.11 |
| 457   | 16.12          | 0.191 83                                     | 0.204 06                                      | -5.99 | 4.48                 | 4.225              | 4.271              |                    |                    | 4.325              | 3.373               | 28.26 |
| 458   | 16.29          | 0.191 83                                     | 0.203 27                                      | -5.63 | 4.472                | 4.191              | 4.108              |                    |                    | 4.257              | 3.352               | 26.98 |
| 459   | 16.45          | 0.191 82                                     | 0.202 55                                      | -5.30 | 4.495                | 4.154              | 4.136              |                    |                    | 4.262              | 3.333               | 27.87 |
| 460   | 16.62          | 0.191 81                                     | 0.201 88                                      | -4.99 | 4.234                | 4.113              | 4.015              |                    |                    | 4.121              | 3.314               | 24.32 |
| 461   | 16.78          | 0.191 80                                     | 0.201 26                                      | -4.70 | 4.268                | 4.127              | 4.123              |                    |                    | 4.173              | 3.296               | 26.58 |
| 462   | 16.95          | 0.191 79                                     | 0.200 67                                      | -4.43 | 4.120                | 3.984              | 4.087              |                    |                    | 4.064              | 3.279               | 23.93 |
| 463   | 17.11          | 0.191 78                                     | 0.200 15                                      | -4.18 | 4.141                | 4.025              | 4.071              |                    |                    | 4.079              | 3.262               | 25.03 |
| 464   | 17.28          | 0.191 78                                     | 0.199 61                                      | -3.92 | 3.991                | 3.815              | 4.037              |                    |                    | 3.948              | 3.246               | 21.64 |
| 465   | 17.44          | 0.191 77                                     | 0.199 13                                      | -3.70 | 3.924                | 3.810              | 3.847              |                    |                    | 3.861              | 3.230               | 19.53 |
| 466   | 17.61          | 0.191 76                                     | 0.198 67                                      | -3.48 | 3.834                |                    | 3.659              |                    |                    | 3.746              | 3.214               | 16.55 |
| 467   | 17.77          | 0.191 75                                     | 0.198 26                                      | -3.28 | 3.883                | 3.743              | 3.782              |                    |                    | 3.803              | 3.199               | 18.86 |
| 468   | 17.94          | 0.191 74                                     | 0.197 86                                      | -3.09 | 3.885                | 3.637              | 3.761              |                    |                    | 3.185              | 18.09               |       |
| 469   | 18.10          | 0.191 73                                     | 0.197 48                                      | -2.91 | 3.979                | 3.653              | 3.717              |                    |                    | 3.783              | 3.171               | 19.30 |
| 470   | 18.27          | 0.191 72                                     | 0.197 13                                      | -2.75 | 3.697                | 3.584              | 3.669              |                    |                    | 3.650              | 3.157               | 15.61 |
| 471   | 18.44          | 0.191 71                                     | 0.196 83                                      | -2.60 | 3.648                | 3.693              |                    |                    |                    | 3.670              | 3.144               | 16.75 |
| 472   | 18.60          | 0.191 69                                     | 0.196 51                                      | -2.45 | 3.719                | 3.558              | 3.540              |                    |                    | 3.606              | 3.131               | 15.18 |



Table 3 (Continued)

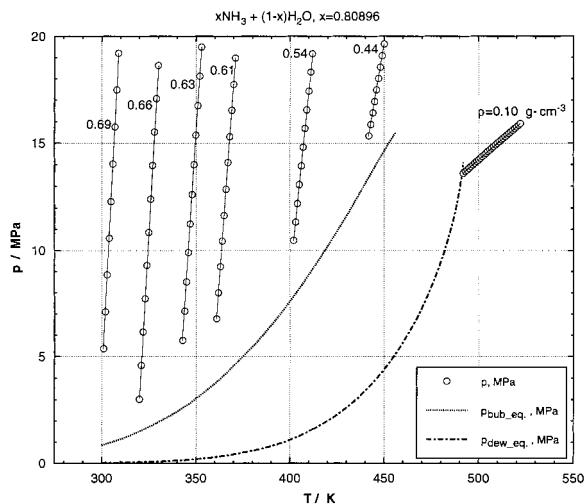
| <i>T</i> /K | <i>p</i> /MPa | $\rho_{\text{exp}}/\text{g}\cdot\text{cm}^3$ | $\rho_{\text{calc}}/\text{g}\cdot\text{cm}^3$ | dev.  | $c_V(\text{no.1})^a$ | $c_V(\text{no.2})$ | $c_V(\text{no.3})$ | $c_V(\text{no.4})$ | $c_V(\text{no.5})$ | $c_{V,\text{avg}}$ | $c_{V,\text{calc}}$ | dev.  |
|-------------|---------------|--|---|-------|----------------------|--------------------|--------------------|--------------------|--------------------|--------------------|---------------------|-------|
| 347         | 9.38          | 0.68547                                      | 0.68558                                       | -0.02 | 3.478                | 3.485              | 3.476              |                    |                    | 3.480              | 3.400               | 2.35  |
| 348         | 10.91         | 0.68529                                      | 0.68552                                       | -0.03 | 3.486                | 3.505              | 3.500              |                    |                    | 3.497              | 3.392               | 3.09  |
| 349         | 12.44         | 0.68512                                      | 0.68545                                       | -0.05 | 3.486                | 3.500              | 3.509              |                    |                    | 3.498              | 3.384               | 3.37  |
| 350         | 13.97         | 0.68495                                      | 0.68537                                       | -0.06 | 3.510                | 3.498              | 3.488              |                    |                    | 3.498              | 3.376               | 3.61  |
| 351         | 15.49         | 0.68477                                      | 0.68528                                       | -0.07 | 3.495                | 3.504              | 3.502              |                    |                    | 3.500              | 3.369               | 3.90  |
| 352         | 17.01         | 0.68460                                      | 0.68520                                       | -0.09 | 3.480                | 3.491              | 3.476              |                    |                    | 3.482              | 3.362               | 3.59  |
| 353         | 18.54         | 0.68442                                      | 0.68511                                       | -0.10 | 3.499                | 3.489              | 3.500              |                    |                    | 3.496              | 3.354               | 4.23  |
| 363         | 5.91          | 0.66000                                      | 0.65996                                       | 0.01  |                      |                    |                    |                    |                    |                    |                     |       |
| 364         | 7.29          | 0.65984                                      | 0.65994                                       | -0.02 |                      |                    |                    |                    |                    |                    |                     |       |
| 365         | 8.68          | 0.65969                                      | 0.65991                                       | -0.03 |                      |                    |                    |                    |                    |                    |                     |       |
| 366         | 10.06         | 0.65953                                      | 0.65987                                       | -0.05 | 3.447                | 3.449              | 3.432              |                    |                    | 3.443              | 3.379               | 1.88  |
| 367         | 11.44         | 0.65938                                      | 0.65982                                       | -0.07 | 3.439                | 3.437              | 3.451              |                    |                    | 3.442              | 3.371               | 2.13  |
| 368         | 12.82         | 0.65922                                      | 0.65977                                       | -0.08 | 3.451                | 3.441              | 3.430              |                    |                    | 3.441              | 3.362               | 2.34  |
| 369         | 14.20         | 0.65907                                      | 0.65971                                       | -0.10 | 3.494                | 3.483              | 3.478              |                    |                    | 3.485              | 3.354               | 3.91  |
| 370         | 15.58         | 0.65891                                      | 0.65964                                       | -0.11 | 3.411                | 3.415              | 3.421              |                    |                    | 3.416              | 3.346               | 2.08  |
| 371         | 16.95         | 0.65876                                      | 0.65957                                       | -0.12 | 3.484                | 3.482              | 3.493              |                    |                    | 3.486              | 3.339               | 4.43  |
| 372         | 18.33         | 0.65861                                      | 0.65950                                       | -0.13 | 3.424                | 3.424              | 3.430              |                    |                    | 3.426              | 3.331               | 2.85  |
| 373         | 19.71         | 0.65845                                      | 0.65942                                       | -0.15 | 3.469                | 3.474              | 3.469              |                    |                    | 3.471              | 3.324               | 4.43  |
| 382         | 7.43          | 0.63225                                      | 0.63209                                       | 0.03  |                      |                    |                    |                    |                    |                    |                     |       |
| 383         | 8.67          | 0.63212                                      | 0.63210                                       | 0.00  |                      |                    |                    |                    |                    |                    |                     |       |
| 384         | 9.90          | 0.63198                                      | 0.63209                                       | -0.02 | 3.388                | 3.401              | 3.411              |                    |                    | 3.400              | 3.376               | 0.71  |
| 385         | 11.13         | 0.63185                                      | 0.63207                                       | -0.04 | 3.442                | 3.428              | 3.398              |                    |                    | 3.423              | 3.367               | 1.66  |
| 386         | 12.36         | 0.63171                                      | 0.63205                                       | -0.05 | 3.428                | 3.436              | 3.442              |                    |                    | 3.435              | 3.358               | 2.31  |
| 387         | 13.59         | 0.63158                                      | 0.63202                                       | -0.07 | 3.433                | 3.415              | 3.435              |                    |                    | 3.428              | 3.349               | 2.35  |
| 388         | 14.82         | 0.63144                                      | 0.63198                                       | -0.09 | 3.399                | 3.397              | 3.406              |                    |                    | 3.401              | 3.340               | 1.82  |
| 389         | 16.05         | 0.63131                                      | 0.63194                                       | -0.10 | 3.419                | 3.419              | 3.452              |                    |                    | 3.430              | 3.332               | 2.95  |
| 390         | 17.28         | 0.63117                                      | 0.63189                                       | -0.11 | 3.400                | 3.416              |                    |                    |                    | 3.408              | 3.323               | 2.55  |
| 391         | 18.51         | 0.63104                                      | 0.63184                                       | -0.13 | 3.397                | 3.404              | 3.386              |                    |                    | 3.396              | 3.315               | 2.42  |
| 392         | 19.74         | 0.63090                                      | 0.63178                                       | -0.14 | 3.389                | 3.468              |                    |                    |                    | 3.429              | 3.307               | 3.67  |
| 412         | 9.19          | 0.58066                                      | 0.57963                                       | 0.18  |                      |                    |                    |                    |                    |                    |                     |       |
| 413         | 10.04         | 0.58057                                      | 0.57943                                       | 0.20  |                      |                    |                    |                    |                    |                    |                     |       |
| 414         | 10.98         | 0.58047                                      | 0.57941                                       | 0.18  |                      |                    |                    |                    |                    |                    |                     |       |
| 415         | 11.94         | 0.58036                                      | 0.5794  | 0.17  |                      |                    |                    |                    |                    |                    |                     |       |
| 416         | 12.91         | 0.58026                                      | 0.57943                                       | 0.14  |                      |                    |                    |                    |                    |                    |                     |       |
| 417         | 13.89         | 0.58016                                      | 0.57945                                       | 0.12  | 3.424                | 3.324              |                    |                    |                    | 3.374              | 3.369               | 0.14  |
| 418         | 14.86         | 0.58005                                      | 0.57947                                       | 0.10  | 3.392                | 3.364              |                    |                    |                    | 3.378              | 3.359               | 0.57  |
| 419         | 15.84         | 0.57995                                      | 0.57948                                       | 0.08  |                      | 3.339              |                    |                    |                    | 3.339              | 3.349               | -0.29 |
| 420         | 16.83         | 0.57984                                      | 0.57948                                       | 0.06  |                      | 3.327              |                    |                    |                    | 3.327              | 3.339               | -0.38 |
| 421         | 17.81         | 0.57974                                      | 0.57947                                       | 0.05  | 3.375                | 3.329              |                    |                    |                    | 3.352              | 3.330               | 0.67  |
| 422         | 18.79         | 0.57964                                      | 0.57945                                       | 0.03  | 3.320                | 3.361              |                    |                    |                    | 3.340              | 3.320               | 0.61  |
| 423         | 19.77         | 0.57953                                      | 0.57944                                       | 0.02  | 3.354                | 3.344              |                    |                    |                    | 3.349              | 3.311               | 1.13  |
| 443         | 14.81         | 0.52545                                      | 0.5229  | 0.49  |                      |                    |                    |                    |                    |                    |                     |       |
| 444         | 15.57         | 0.52537                                      | 0.52295                                       | 0.46  |                      |                    |                    |                    |                    |                    |                     |       |
| 445         | 16.31         | 0.52529                                      | 0.52295                                       | 0.45  |                      | 3.421              |                    |                    |                    | 3.421              | 3.410               | 0.31  |
| 446         | 17.07         | 0.52521                                      | 0.52295                                       | 0.43  |                      |                    | 3.358              | 3.387              |                    | 3.373              | 3.399               | -0.77 |
| 447         | 17.82         | 0.52514                                      | 0.52294                                       | 0.42  | 3.360                | 3.328              |                    |                    |                    | 3.344              | 3.387               | -1.28 |
| 448         | 18.57         | 0.52506                                      | 0.52293                                       | 0.41  | 3.299                | 3.253              | 3.268              |                    |                    | 3.273              | 3.376               | -3.06 |
| 449         | 19.33         | 0.52498                                      | 0.52291                                       | 0.40  |                      | 3.312              | 3.318              |                    |                    | 3.315              | 3.365               | -1.50 |
| 465         | 15.65         | 0.46455                                      | 0.45801                                       | 1.43  |                      |                    |                    |                    |                    |                    |                     |       |
| 466         | 16.18         | 0.46450                                      | 0.45773                                       | 1.48  | 3.506                | 3.497              |                    |                    |                    | 3.502              | 3.538               | -1.03 |
| 467         | 16.72         | 0.46444                                      | 0.45748                                       | 1.52  |                      | 3.479              |                    |                    |                    | 3.479              | 3.525               | -1.30 |
| 468         | 17.26         | 0.46439                                      | 0.45726                                       | 1.56  |                      | 3.452              |                    |                    |                    | 3.452              | 3.512               | -1.69 |
| 469         | 17.80         | 0.46434                                      | 0.45705                                       | 1.60  | 3.400                | 3.378              |                    |                    |                    | 3.389              | 3.498               | -3.13 |
| 470         | 18.35         | 0.46428                                      | 0.45686                                       | 1.62  | 3.328                | 3.294              |                    |                    |                    | 3.311              | 3.486               | -5.01 |
| 471         | 18.90         | 0.46422                                      | 0.45669                                       | 1.65  | 3.305                | 3.319              |                    |                    |                    | 3.312              | 3.473               | -4.62 |
| 472         | 19.45         | 0.46417                                      | 0.45652                                       | 1.68  |                      | 3.236              |                    |                    |                    | 3.236              | 3.460               | -6.47 |

<sup>a</sup> All  $c_V$  values in  $\text{kJ}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$ .

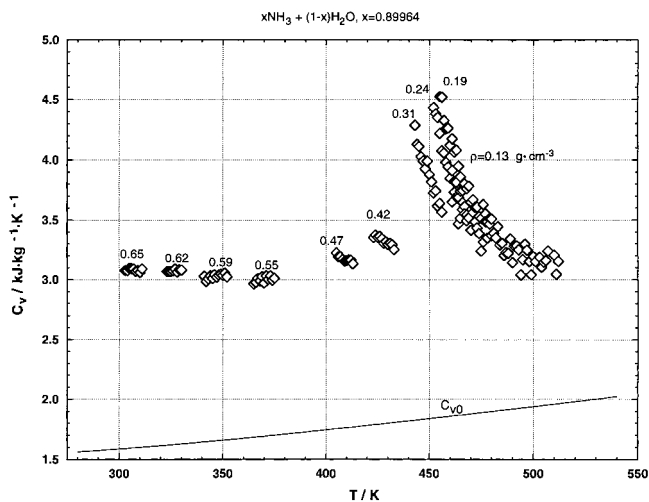
which leaves only a narrow gap above the bubble-point pressures at temperatures above about 425 K. Figures 2, 4, and 6 show the measured specific heat capacities for each of the compositions. At densities  $\rho > \sim 1.3\rho_c$ , the liquid-phase  $c_V$  values show only weak dependence on both density and temperature with the appearance of a shallow minimum heat capacity. The minima range from about (3.0 to 3.3)  $\text{kJ}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$  as the mole fraction ( $x$ ) of ammonia decreases from 0.9 to 0.7 in the mixture. Compressed-gas heat capacities for the  $x \approx 0.8$  and  $x \approx 0.9$  mixtures show a significantly stronger rate of change with temperature. In this case, the  $c_V$  values range from (2.7 to 4.5)  $\text{kJ}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$ .

As shown in Table 2, the uncertainty of values of  $c_V$  for gases is about four times that for liquid-phase results. This

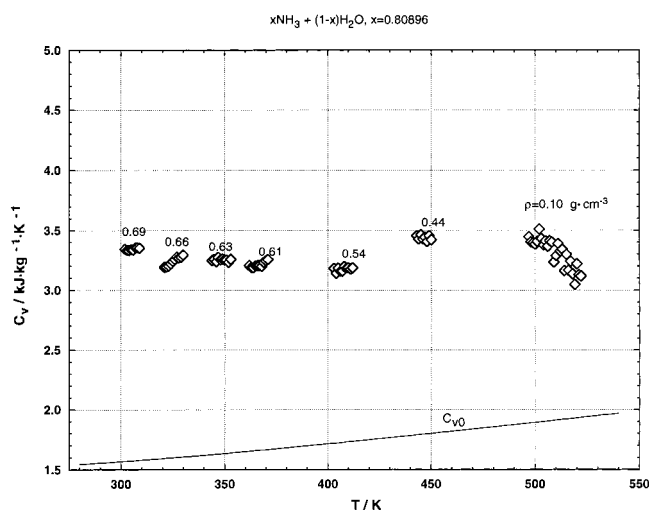
is due to the higher relative uncertainty of the  $\Delta Q$  term for gaseous measurements. Consequently, the gas-phase  $c_V$  data have considerably more scatter than the liquid-phase data. Figures 2 and 4 indicate that this scatter is a factor of about 10 larger in the gas than in the liquid. We think that this scatter is due to the combination of two effects. The first is the considerably higher electrical noise originating with thermal EMFs at temperatures above 425 K. The second is the much lower measured energy changes, which were a factor of 10 smaller than for liquid-phase samples. While we can certainly conceive techniques to reduce noise, the second effect cannot be mitigated for an apparatus of fixed volume. Electrical noise destabilizes the control algorithm and causes spurious losses or gains of energy that cannot be calculated. This noise arises when



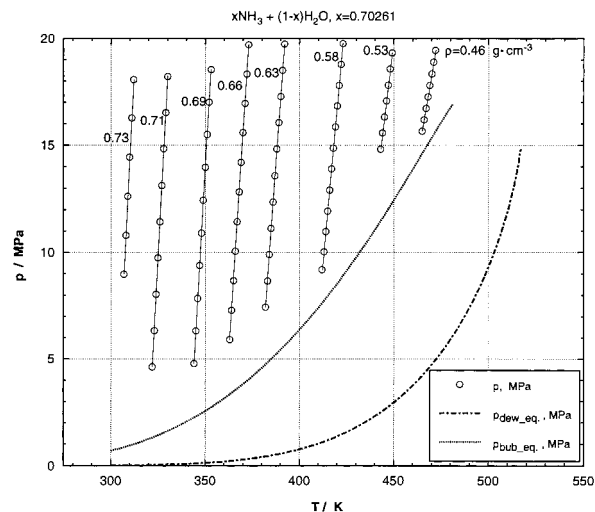
**Figure 1.** Measured pressure and temperature states along isochores for  $\{x\text{NH}_3 + (1-x)\text{H}_2\text{O}, x = 0.80896\}$ , showing the dew-bubble curves calculated with a formulation by Tillner-Roth and Friend (1998b).



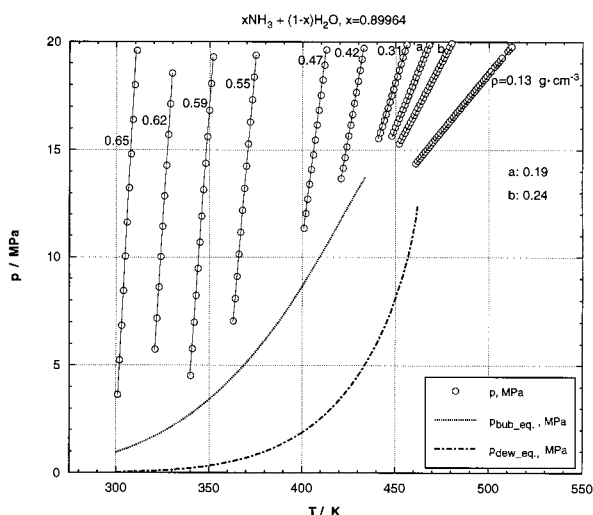
**Figure 4.** Measured specific heat at constant volume  $c_V$  for  $\{x\text{NH}_3 + (1-x)\text{H}_2\text{O}, x = 0.89964\}$ , showing the ideal gas heat capacity  $C_V^0$  calculated with a formulation by Tillner-Roth and Friend (1998b).



**Figure 2.** Measured specific heat at constant volume  $c_V$  for  $\{x\text{NH}_3 + (1-x)\text{H}_2\text{O}, x = 0.80896\}$ , showing the ideal gas heat capacity  $C_V^0$  calculated with a formulation by Tillner-Roth and Friend (1998b).



**Figure 5.** Measured pressure and temperature states along isochores for  $\{x\text{NH}_3 + (1-x)\text{H}_2\text{O}, x = 0.70261\}$ , showing the dew-bubble curves calculated with a formulation by Tillner-Roth and Friend (1998b).

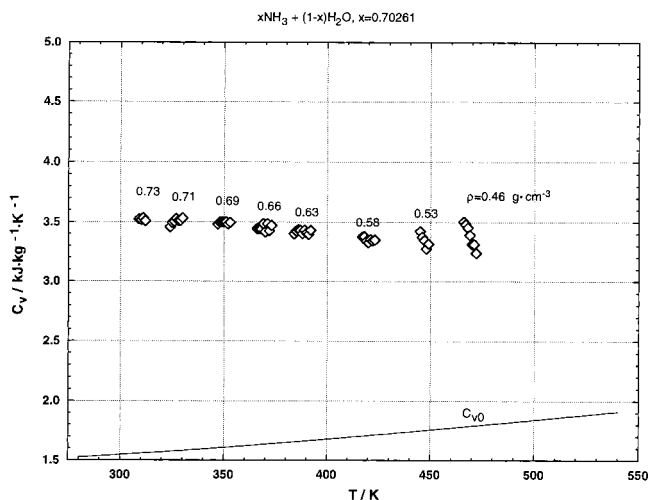


**Figure 3.** Measured pressure and temperature states along isochores for  $\{x\text{NH}_3 + (1-x)\text{H}_2\text{O}, x = 0.89964\}$ , showing the dew-bubble curves calculated with a formulation by Tillner-Roth and Friend (1998b).

crimped electrical connections loosen at elevated temperatures. Loose connectors generate electrical noise, which can swamp the nanovolt signals that we are attempting to measure. For future studies, modifications are being made to reduce thermal emfs in the measuring circuits by replacing crimped connectors with cleaned and carefully soldered connections. Preliminary tests lead us to be optimistic that this will decrease the scatter of gas-phase  $c_V$  to a more satisfactory value.

Table 3 presents comparisons of calculated densities and heat capacities with experimental values from this work. The calculations were made with a formulation developed by Tillner-Roth and Friend (1998b). This formulation was developed by using published thermodynamic measurements that were available at temperatures up to 334 K for heat capacity and up to 413 K for density. Above such temperatures, the calculations are an extrapolation of the available data along the lines of the formulation. Table 3 shows that the calculated densities are within  $\pm 0.3\%$  at temperatures up to 400 K, within  $\pm 8\%$  in the extended critical region, and within  $\pm 0.6\%$  in the supercritical gas region. Also, Table 3 shows that the calculated heat





**Figure 6.** Measured specific heat at constant volume  $c_V$  for  $\{x\text{NH}_3 + (1-x)\text{H}_2\text{O}, x = 0.70261\}$ , showing the ideal gas heat capacity  $c_V^0$  calculated with a formulation by Tillner-Roth and Friend (1998b).

capacities are within  $\pm 5\%$  at all state conditions except the extended critical and supercritical gas regions, where they are within  $\pm 30\%$ . Since the present data were not available to Tillner-Roth and Friend, it is perhaps not surprising that the deviations often exceed the uncertainty of the measurements. On the other hand, considering how most of the calculated densities and heat capacities are an extrapolation of the published data, the agreement of the calculations with experiment is good.

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